

Differential equation has the following physical basis. If x - amount of substance P, formed at time t , then the problem comes from the conditions that this point of time the reaction came substance A and substance B. This in turn means that up to this point and not left reacted substance A and substance B.

According to the law of mass action, for simple chemical reactions, reaction conditions for the first stage, the rate of chemical interaction v is proportional to the concentration of the reactants, ie, either.

For ease up a table matching objectives and conditions designations following entry method Runge-Kutta (tab. 4.2).

Table 4.2. Compliance markings

Terms problem number Runge-Kutta method of discrete analog Analytical Account
1

$$VI \quad VI + 1 = \Delta u_i + y' = f(x, y)$$

$$2 \quad x = x(t) \quad VI \quad y = f(x)$$

$$3 \quad t \quad x_i \quad x$$

$$4 \quad x(t_0) = x_0 \quad y_0 \quad y(x_0) = y_0$$

$$(t, x) f^5$$

To illustrate the calculations by the method of Runge-Kutta for example, when according to the task (all dimensions - conventional): $t_0 = 0,1$; $x_0 = 0,1$; $k(t) = 2 \cdot t$; $h = 0,01$; the observation $t_{max} = 10$.

According to Runge-Kutta method for tabular dependence x_i perform the following steps.

Initial conditions: $i = 0$; $t_0 = 0,1$; $x_0 = 0,1$.

$$\cdot x_0) = 2 \cdot 0,1 \cdot (1 - 1 / 1,5 \cdot 0,1) \cdot (0,5 - \chi / \beta - \beta \cdot x_0) \quad (\chi / \alpha - \alpha(t_0, x_0) = 2 \cdot t_0 \cdot (f \cdot 0,5 / 1,5 \cdot 0,1) = 0,0759;$$

$$(t_0, x_0) = 0,01 \cdot 0,0759 = 0,000759; fA_0 = h \cdot$$

$$\cdot (x_0 + A_0 / 2)) = \chi / \beta - \beta \cdot (x_0 + A_0 / 2)) \quad (\chi / \alpha B_0 = h \cdot (t_0 + h / 2) \cdot (a - 0,1 \cdot (0,1 + 0,1 / 2) \cdot (1 - 1 / 1,5 \cdot (0,1 + 0,000759 / 2)) \cdot (0,5 - 0,5 / 1,5 \cdot (0,1 + 0,000759 / 2)) = 0,0046;$$

$$\cdot (x_0 + B_0 / 2)) = \chi / \beta - \beta \cdot (x_0 + B_0 / 2)) \quad (\chi / \alpha C_0 = h \cdot (t_0 + h / 2) \cdot (a - 0,1 \cdot (0,1 + 0,1 / 2) \cdot (1 - 1 / 1,5 \cdot (0,1 + 0,0046 / 2)) \cdot (0,5 - 0,5 / 1,5 \cdot (0,1 + 0,0046 / 2)) = 0,0007;$$

$$\cdot (x_0 + B_0)) = \chi / \beta - \beta \cdot (x_0 + B_0)) \quad (\chi / \alpha D_0 = h \cdot (t_0 + h / 2) \cdot (a - 0,1 \cdot (0,1 + 0,1 / 2) \cdot (1 - 1 / 1,5 \cdot (0,1 + 0,0007)) \cdot (0,5 - 0,5 / 1,5 \cdot (0,1 + 0,0007)) = 0,0007;$$

$$\Delta x_0 = 1/6 \cdot (A_0 + 2V_0 + 2S_0 + D_0) = 1/6 \cdot (0,000759 + 2 \cdot 0,0046 + 2 \cdot 0,0007 + 0,0007) = 0,001214; x_1 = x_0 + \Delta x_0 = 0,1 + 0,001214 = 0,101214$$

The next step: $i = 1$; $t_1 = t_0 + 1 \cdot h = h$.

You must complete all the steps again consistently for all nodes i .

Recursive actions require too much computation, so they should perform on a PC in the cyclic calculation algorithms. Calculation program (written in free form location operators) and table IDs (table 4.3.) Provided an example below.

Table 4.3. Table Match identifiers.

For number

In the text

Numerical program

Record Type importance

1 t0 T0 0,1 REAL .1

2 h h 0,01 REAL .01

3 k (t) Function Ak (t) calculated REAL -

4

Alpha 1 REAL 1.

5

Beta 0,5 REAL .5

Chi Calculated REAL - χ 6

7 tmax Tmax 10 10 REAL.

8 x0 X0 0,1 REAL .1

Calculated 9 Ai A REAL -

10 Bi B is calculated REAL -

11 Ci C Calculated REAL -

12 Di D calculated REAL -

(t, x) Function f 13

(t, x) calculated REAL -f

14 t t calculated REAL -

15 x x Calculated REAL -

16 i i Calculated INTEGER -

17 - Dx calculated REAL -

! The source code program for calculating chemical reaction

Module M1! Expanding the area of variable visibility

Real Alpha /1./, Beta /.5/, Chi

End Module M1

!

Function Ak (t)! k (t) - see. task

$Ak = 2 * t$

End Function Ak

!

Function f (t, x)! The right side of the differential equation (see. Diffusion. Model)

USE M1! Access to data module by name

Chi = Alpha + Beta

$f = Ak(t) * (Alpha - Alpha / Chi * x) * (Beta - Beta / Chi * x)$

End Function f

!

Program Chemical! The main program

Data T0 / .1 /, X0 / .1 /, Tmax / 200. /, h / .1 /! Output (see. Task)

Open (1, File = 'Chemi.txt', Status = 'Replase')! File calculation results

Write (1, *) '***** Inputed Data *****'

Write (1, *) 'T0 =', T0

Write (1, *) 'x0 =', X0

Write (1, *) 'Tmax =', Tmax

Write (1, *) 'h =', h

Write (1, *) '***** Solved Resalts *****'

```

Write (1, *) 'i t x!' Table caps
i = 0; t = T0; x = X0! The initial conditions
Write (1, *) i, t, x! To file
Do t = T0 + h, Tmax + h, h! Cycle calculation formula Runge-Kutta
i = i + 1
A = h * f (t, x)
B = h * f (t + h / 2, x + A / 2)
C = h * f (t + h / 2, x + B / 2)
D = h * f (t + h / 2, x + C)
Dx = (A + B * 2 + 2 * * C + D)
x = x + Dx
Write (1, *) i, t, x! To file
EndDo! End cycle
Write (1, *) '_____ '
Stop
End

```

Project MS Dev FPS4 of software code and the calculation results are shown in Figure 4.3.

Fig. 4.3. Project MS Dev FPS4 of software code and the calculation results

Results of calculation of transfer to Excel (Fig. 4.4) for further engineering analysis.

Fig. 4.4. Display Excel chart to change the number of calculations Chemicals reaction in time