

# N.m.r. relaxation in Nafion—the low temperature regime

Bryce MacMillan\*, Allan R. Sharp, Robin L. Armstrong

*Physics Department, University of New Brunswick, P.O. Box 4400, Fredericton, New Brunswick, Canada E3B 5A3*

Received 28 April 1997; revised 8 June 1998; accepted 15 June 1998

## Abstract

The dynamical characteristics of water absorbed in Nafion are investigated using n.m.r. At temperatures below the dynamical transition temperature,  $T_t$ , relaxation rates indicate mobility associated with a fluid but the derived motional activation energies are similar to those of ice. This indicates a well ordered supercooled fluid consisting of hydrogen bonded water structures. The correlation time  $\tau_c$  is found to have a Gaussian dependence on the surface area to volume ratio, unlike simple porous systems. We have shown that the surface area depends on  $r^{2.5}$ . We feel that this is due to the irregular nature of the surfaces of the clusters. © 1999 Published by Elsevier Science Ltd. All rights reserved.

*Keywords:* N.m.r.; Nafion; Relaxation

## 1. Introduction

The dynamical behaviour of water absorbed in Nafion, as observed by n.m.r. relaxation, exhibits several unique features, as discussed in the previous paper [1]. Among these is an observed transition in the relaxation characteristics at a specific temperature, denoted,  $T_t$ . At temperatures above this transition, the absorbed water behaves very much like bulk water, and is modified only slightly by the presence of the polymer. The previous paper presents a detailed analysis of the relaxation of this regime.

At temperatures below this transition, the relaxation behaviour indicates significant change to the dynamical characteristics of the absorbed water. This paper discusses the nature of these dynamics. Nafion, sample preparation and experimental methods are described elsewhere [1].

It is well established that the nuclear magnetic relaxation rate of a gas or liquid is enhanced near an interface to a solid [2]. The correlation times of molecules at the surface,  $\tau_{cs}$ , are generally longer than those in the bulk,  $\tau_{cb}$ . The specific mechanism for the enhancement is generally not well understood, but it has been speculated that it is due either to the presence of paramagnetic sites on the solid surface or to the attractive van der Waals force between liquid and solid at the interface which hinders the molecular dynamics [3].

Magnetization evolution in confining pores is commonly modelled based on the work of Brownstein and Tarr [4], who investigated relaxation as a function of diffusion and

geometry. Their results indicate that the observed relaxation is the average of the fluid and surface relaxation, weighted by the surface area to volume ratio. Using their approach, n.m.r. has been successfully employed as a probe of pore structure and size in saturated porous media, including oil sands [5], sedimentary rock [6–9] and porous glass [10,11]. There have also been several modifications reported recently which give extra consideration to bulk relaxation [12], consider a distribution of pore sizes [13], and expand the theory to encompass pulse field gradient techniques [14].

These models fail to describe the observed behaviour of water absorbed in Nafion. In this paper, a different approach is reported.

## 2. Analysis of the low temperature data

In this temperature regime, the characteristics of the data more closely resemble those predicted by the BPP [15] relaxation theory (see Fig. 1) than do the high temperature data. The minimum in the  $T_1$  data and the convergence of the three data sets at higher temperatures are features of BPP relaxation. There are, however, two significant deviations from this relaxation model. The BPP theory predicts the existence of a minimum in  $T_{1\rho}$ . For a spin-locking field strength of 10 Gauss, the value of  $T_{1\rho}$  at the minimum is expected to be lower than the minimum value of  $T_1$  by a factor of 185. We did not observe the expected minima in the  $T_{1\rho}$  data.

\* Corresponding author. Tel.: +1-506-453-4723; Fax +1-506-453-4581.

Also, the BPP relaxation model predicts that  $T_2$  decreases monotonically with  $\beta$  ( $\beta = 1000/T$ ). The data for the Nafion–water systems show distinct changes in the dependence of  $T_2$  on  $\beta$ . Clearly, further contributing factors to the relaxation are indicated.

Goldmann–Shen [16] and Selective Inversion experiments were performed to detect the presence of cross-relaxation between the solid-like and liquid-like environments. No cross-relaxation was detected.

Above  $T_t$ , previous analysis [1] has suggested that the small fraction of protons associated with the ionic groups contribute to the observed  $T_2$  and  $T_{1\rho}$  relaxation behaviour. We expect a similar phenomenon to occur below  $T_t$ , but with a distinction. The  $\text{SO}_3\text{H}$  group becomes dissociated because of the large difference in the density of states between the  $\text{SO}_3\text{H}$  group and the water. That is, there are many more states available to the radical in solution than there are when it is attached to the backbone, and the equilibrium is biased very much towards the dissociated state. However, with decreasing temperatures, the density of states available in the water decreases very rapidly, and the equilibrium begins to favour the solid state. It is our suggestion that there is a temperature range over which the  $\text{SO}_3\text{H}$  groups go from being essentially fully dissociated to being fully associated. Below this temperature range, there is a large fraction of protons in a solid-like environment which contribute to the observed  $T_2$  and  $T_{1\rho}$  relaxation.

This temperature range will be defined by the properties of the absorbed water, which are functions of level of hydration. For simplicity it is assumed that the fraction of protons in solid-like sites increases linearly with temperature throughout this range. The observed relaxation rates are simply the weighted averages of the relaxation rates from the protons in solid-like and liquid-like environments. Relaxation of the protons in liquid-like sites is modelled using the BPP theory [15]. The motional correlation time,  $\tau_c$ , is assumed to have an Arrhenius dependence on temperature.

The breadth of the minimum in  $T_1$  indicates that a distribution of correlation times is required, so that

$$\frac{1}{T_1} = \int_0^{\infty} \frac{P(\tau_c)}{T_1(\tau_c)} d\tau_c \quad (1)$$

Similar expressions describe the rates  $1/T_2$  and  $1/T_{1\rho}$ . For  $P(\tau_c)$ , it is common to assume a log-normal distribution [17] of the form

$$P(\tau_c) = \frac{\lambda}{\pi^{1/2}} e^{-s^2/\lambda^2} \quad (2)$$

where

$$S = \ln\left(\frac{\tau_c}{\bar{\tau}_c}\right) \quad (3)$$

and

$$\lambda^2 = \lambda_0^2 + \left(\frac{\lambda_Q}{RT}\right)^2 \quad (4)$$

with  $\lambda$  a parameter describing the width of the distribution,

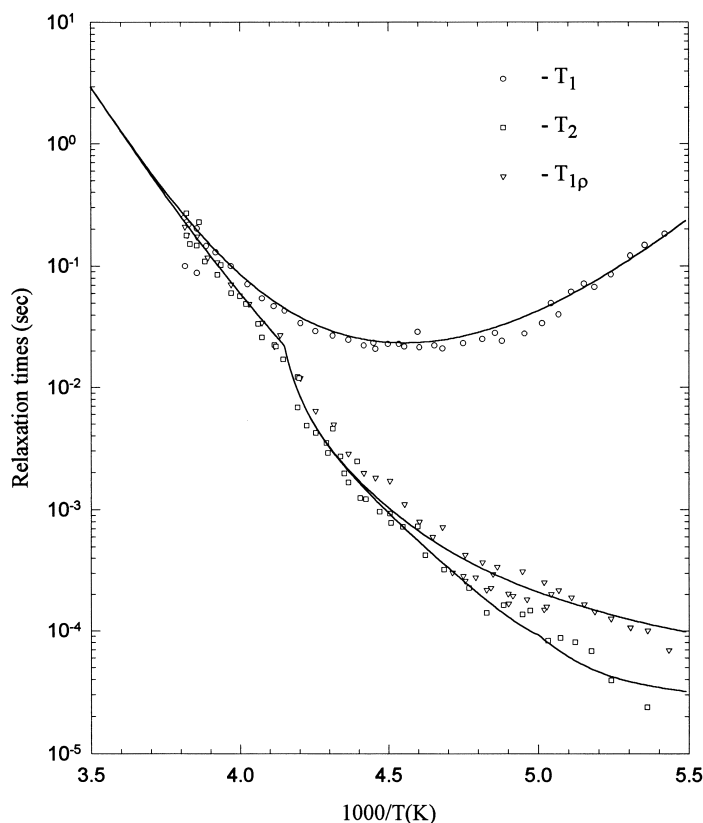


Fig. 1. Nafion hydrated to 15.9%  $\text{H}_2\text{O}$ . The solid lines represent the best fit to the model described in the text.

Table 1  
Relaxation parameters associated with the liquid-like phase

Hydration level (%)	$\tau_o$ (s)	$E_a$ (kcal)	$\lambda_o, \lambda_Q$
15.9	$(7.9 \pm 0.5) \times 10^{-24}$	$14.5 \pm 0.4$	$3.2 \pm 0.3, 0$
7.7	$(4.8 \pm 0.7) \times 10^{-23}$	$14.2 \pm 0.5$	$3.2 \pm 0.3, 0$
5.9	$(8.5 \pm 0.9) \times 10^{-23}$	$14.5 \pm 0.7$	$3.5 \pm 0.5, 0$
3.0	$(6.4 \pm 0.9) \times 10^{-21}$	$14.0 \pm 0.8$	$3.8 \pm 0.6, 0$
1.8	$(1.7 \pm 0.4) \times 10^{-19}$	$13.6 \pm 1.0$	$4.1 \pm 0.8, 0$
8.5 D <sub>2</sub> O	$(4.4 \pm 1.5) \times 10^{-24}$	$15.0 \pm 1.0$	$3.1 \pm 0.8, 0$

and  $\lambda_o$  and  $\lambda_Q$  the temperature independent and dependent contributions.

For the protons in solid-like sites, a single isotropic site is used. The motional correlation time is also assumed to have an Arrhenius temperature dependence. As is commonly done with this type of modelling, a lower limit was imposed on the value of  $T_2$ . This marks the onset of the rigid-lattice regime, in which  $T_2$  changes very little; a value of 10  $\mu$ s was used. The results of the modelling for Nafion hydrated to 15.9% H<sub>2</sub>O are presented in Fig. 1. The solid lines represent the best fit of the model to the data. The change in the slope of the  $T_2$  and  $T_{1\rho}$  data coincides with the beginning of the reassociation of the acid groups. The parameters derived for the liquid-like relaxation are given in Table 1.

In this temperature regime the characteristics of the water absorbed in Nafion are somewhat anomalous. The activation energies deduced for the reorientational motion are large. Typically, O–H···O hydrogen bonds have energies of 3.5–4 kcal/mole. Within this phase, molecular reorientation requires the breaking of up to four hydrogen bonds. This high degree of bonding is indicative of a highly ordered phase. Similar behaviour is observed in normal ice [18], where four hydrogen bonds must be broken to accommodate reorientation.

Due to the temperature range involved and the peculiar ordered structure it is tempting to equate this water phase with ice. Ice, however, is characterized by a correlation time of approximately  $10^{-6}$  s and is very rigid. This is reflected in a very short  $T_2$  of several  $\mu$ s. Within this water phase, the observed  $T_2$  is as high as 200 ms, and the calculated correlation time at  $-20^\circ\text{C}$  varies between samples from  $10^{-10}$  to  $10^{-11}$  s.

Water in this phase is a well-ordered supercooled fluid. Mobility is less than in either free water or the high temperature regime discussed in the previous paper, but much greater than in ice. It is our belief that water is forming

complex cage-like structures, or clathrates, consisting of many molecules, and it is these we are seeing. Compound water within Nafion has previously been observed with infrared techniques [19–21]. Supercooling is maintained at much lower temperatures than expected for water in regular porous geometries [22]. It is believed that the irregularly shaped clusters within Nafion facilitate this supercooling. Modification is due to the presence of the surface. In these systems, the surface area to volume ratio is much higher than in simple geometries.

### 3. Variation with hydration

The results from Nafion hydrated to 7.7% H<sub>2</sub>O are presented in Fig. 2. Similar features are noted at all levels of hydration. It is significant that within the liquid-like phase the motional activation energy and the breadth of the distribution in  $\tau_c$  are invariant between samples. This indicates uniformity in the underlying relaxation processes. The dynamical mechanisms are independent of pore size; only the timescale is affected. The modifications in timescale, i.e. to the motional correlation times, are the result of changes in the ratio of surface area to volume within the clusters.

The moderating effects of the confining pores on the dynamical behaviour of the water can best be studied by examining the dependence of the motional correlation time  $\tau_c$  on pore size. For illustrative purposes,  $\tau_c$  has been calculated at  $-20^\circ\text{C}$  for all samples. This has been recorded in Table 2.

Existing models describing relaxation in porous geometries [4–14] fail in these Nafion–water systems. They predict that the observed relaxation is the weighted sum of relaxation from two regions, effectively a bimodal distribution of correlation times. The effect of altering the respective weighting in a bimodal distribution, as would

Table 2  
The correlation time  $\tau_c$  and pore size in Nafion at  $-20^\circ\text{C}$

Hydration level (%)	Hydration level ( <i>n</i> )	Pore diameter ( $\text{\AA}$ )	$\tau_c$ (s) 253°K
15.9	11.6	27	$6.5 \times 10^{-12}$
7.7	5.1	23	$8.7 \times 10^{-11}$
5.9	3.8	22	$2.8 \times 10^{-10}$
3.0	1.9	21	$7.8 \times 10^{-9}$
1.8	1.1	20	$6.6 \times 10^{-7}$
8.5 D <sub>2</sub> O	5.1	23	$3.9 \times 10^{-11}$

happen with varying hydration, is a marked change in the shape and width of the corresponding minimum in  $T_1$ . Such changes are absent from our data.

These models fail for several reasons, but we believe that the most important factor is the irregular nature of the surface of the pores in the Nafion–water systems. It has been indicated [19,23] that there is a high degree of intrusion of the fluorocarbon matrix into the pores. The resulting ‘fuzzy’ spheres have a ratio of surface area to volume considerably higher than for a perfect sphere. There is not an obvious distinction between a surface layer and a bulk phase. Instead, there is effectively one phase in which all water molecules spend some fraction of the time at or near a surface.

It is felt that the higher than average surface area within these pores is also the characteristic which inhibits the formation of ice at these low temperatures. This conclusion is based on the results of neutron scattering experiments on water absorbed in porous glass [24], where the confining geometries are less favourable to the formation of long orderly hexagonal channels which accompany the formation of hexagonal ice.

The dynamical behaviour, including the average reorientational correlation time, is a function of the fraction of time spent in proximity to the fluorocarbon phase. This is also observed in viscosity [25] and heat capacity [26] measurements of absorbed fluids, where these quantities are observed to increase in the vicinity of confining surfaces.

The pore size dependence of the correlation times observed in hydrated Nafion can be described by an empirical relationship. The bulk correlation time,  $\tau_0$ , is modified by the presence of the surface to an extent dependent upon the fraction of time spent by water molecules in proximity to the surface. This is directly related to the amount of surface area available to each molecule, or the surface area to volume ratio. For a spherical pore, the volume is proportional to  $r^3$  and the surface area is proportional to  $r^2$ . For a fuzzy sphere, this volume relation still holds if  $r$  is taken as an appropriate effective radius. The surface area, however, is directly affected by the degree of fuzziness, and the surface relation must be modified accordingly. It is assumed that the surface area is proportional to  $r^n$ . The surface area to volume ratio is then proportional to  $r^{n-3}$ . Further, it is assumed that there is a maximum value of surface area available to each water molecule. This is reflected in a minimum radius,  $r_0$ . The observed correlation times are fit to a Gaussian dependence

$$\tau = \tau_0 e^{Cx^2} \quad (5)$$

where

$$x = \left( \frac{r - r_0}{r_0} \right)^{n-3} \quad (6)$$

The denominator in Eq. (6) has been introduced to make  $x$  dimensionless. From the previous paper,  $r_0 = 9.7 \text{ \AA}$ . The best fit to the data yields  $\tau_0 = 9.1 \times 10^{-13} \text{ s}$ ,  $C = 0.74$ , and

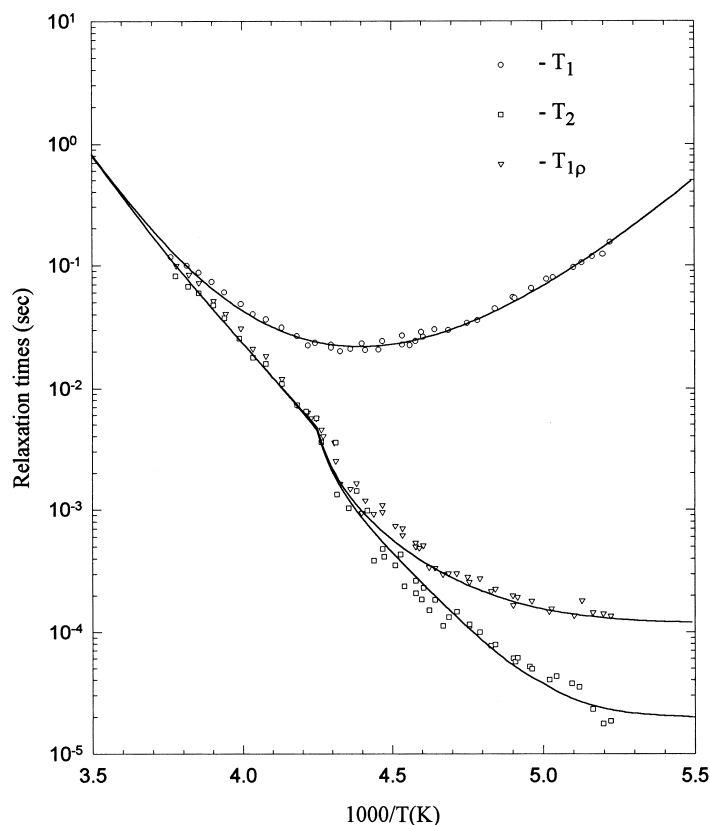


Fig. 2. Nafion hydrated to 7.7%  $\text{H}_2\text{O}$ . The solid lines represent the best fit to the model described in the text.

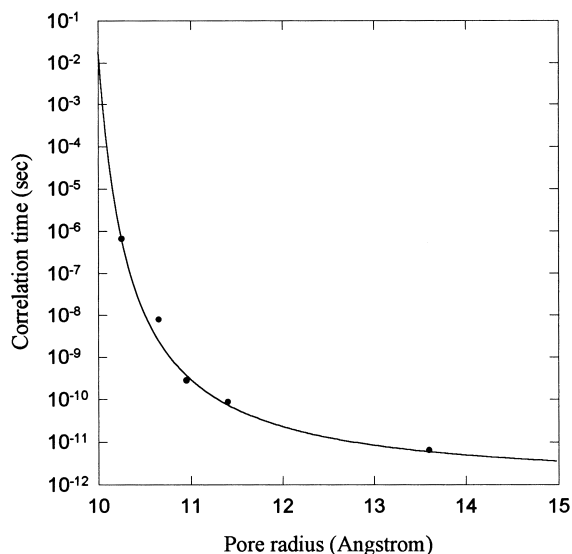


Fig. 3. The calculated correlation time in Nafion at  $-20^{\circ}\text{C}$  as a function of pore radius.

$n = 2.5$ . This is presented in Fig. 3. Although it is difficult to extract reliable parameters from only five data points, the value obtained for  $\tau_0$  agrees well with the expected value for bulk water [27] of approximately  $10^{-12}$  s.

The value obtained for the exponent  $n$  supports the view of the irregularly shaped cluster surfaces within Nafion. For a spherical pore, surface area is proportional to  $r^2$  and volume is proportional to  $r^3$ . From the present results, the cluster surface area is proportional to  $r^{2.5}$ . As previously hypothesized, the surface area to volume ratio of the clusters within Nafion is unusually high.

The significant result of this exercise is that the motional correlation time of the water absorbed in Nafion clusters has a Gaussian dependence on the surface area to volume ratio. This has not been observed with conventional porous materials, and indicates that the irregularities inherent to the surface of the Nafion cluster dramatically alter the dynamical properties of the water.

In this low temperature regime, water absorbed in Nafion is characterized differently than in the high temperature extreme where its behaviour mimics that of bulk water. Here, water structures are formed, consisting of many

molecules in well ordered clathrates with a high degree of hydrogen bonding, yet maintaining fluid-like dynamics. The irregular surfaces of the pores determine to a large extent the dynamical properties of the absorbed water, in particular the motional correlation time  $\tau_c$ . They are also believed responsible for the apparent extreme supercooling.

## References

- [1] MacMillan B, Sharp AR, Armstrong RL. *Polymer* 1999;40:2471.
- [2] Chapman R, Bloom M. *Can J Phys* 1975;54:861.
- [3] Halperin WP, D'Orazio F, Bhattacharja S, Tarczon JC. In: Klafter J, Drake JM, editors. *Molecular dynamics in restricted geometries*. New York: Wiley, 1989.
- [4] Brownstein KR, Tarr CE. *Phys Rev A* 1979;19:2446.
- [5] Davies S, Kalam MZ, Packer KJ, Zelaya FO. *J Appl Phys* 1990;67:3171.
- [6] Cohen MH, Mendleson KS. *J Appl Phys* 1982;53:1127.
- [7] Chen R, Stallworth PE, Greenbaum SG, Kleinberg RL. *J Mag Res A* 1994;110:77.
- [8] Lipsicas M, Banavar JR, Willemsen J. *Appl Phys Lett* 1986;48:1544.
- [9] Mendelson KS. *J Appl Phys* 1982;53:6456.
- [10] D'Orazio F, Tarczon JC, Halperin WP, Eguchi K, Mizusaki T. *J Appl Phys* 1989;65:742.
- [11] D'Orazio F, Bhattacharja S, Halperin WP, Eguchi K, Mizusaki T. *Phys Rev B* 1990;42:9810.
- [12] Davies S, Packer KJ. *J Appl Phys* 1990;67:3163.
- [13] McCall KR, Johnson DL, Guyer RA. *Phys Rev B* 1991;44:7344.
- [14] McCall KR, Guyer RA, Johnson DL. *Phys Rev B* 1993;48:5997.
- [15] Abragam A. *Principles of nuclear magnetism*. Oxford: Clarendon Press, 1948.
- [16] Goldman M, Shen L. *Phys Rev* 1966;144:321.
- [17] Connor TM. *Trans Farad Soc* 1964;50:1674.
- [18] Hasted JB. In: Franks F, editor. *Water, a comprehensive treatise*, vol. 1. New York: Plenum, 1972.
- [19] Falk M. In: Eisenberg A, Yeager Y, editors. *Perfluorinated ionomer membranes*. Washington, DC: American Chemical Society, 1982.
- [20] Ostrowska J, Narebska A. *Coll and Polym Sci* 1983;261:93.
- [21] Ostroska J, Narebska A. *Coll and Polym Sci* 1984;262:305.
- [22] Angell CA. In: Franks F, editor. *Water, a comprehensive treatise*, vol. 7. New York: Plenum, 1982.
- [23] Falk M. *Can J Chem* 1980;58:1495.
- [24] Bellissent-Funel MC, Lal J, Bosio L. *J Chem Phys* 1993;98:4246.
- [25] Malik M, Letey J. *Soil Sci Soc Am J* 1992;56:1032.
- [26] Etzler FM. *Langmuir* 1988;4:878.
- [27] Sciortino F, Poole PH, Stanley HE, Halvin S. *Phys Rev Lett* 1990;64:1686.